

Theoretical investigations on molecular structure, NBO, HOMO-LUMO and MEP analysis of two crystal structures of *N*-(2-benzoyl-phenyl) oxalyl: A DFT study

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ABSTRACT

The *N*-(2-benzoyl-phenyl) oxalyl derivatives are important models for studying of three-centered intramolecular hydrogen bonding in organic molecules. The quantum theoretical calculations for two crystal structures of *N*-(2-benzoyl-phenyl) oxalyl (compounds **I** and **II**) were performed by Density Functional Theory (B3LYP method and 6-311+G* basis set). From the optimized structures, geometric parameters were obtained and experimental measurements were compared with the calculated data. The NMR parameters such as chemical shift isotropic (CS^I) and chemical shift anisotropic (CS^A), natural charge (NBO), thermodynamic parameters such as relative energy (ΔE), standard enthalpies (ΔH), entropies (ΔS), Gibbs free energy (ΔG) and constant volume molar heat capacity (C_v), frontier molecular orbitals (FMOs), total density of states (DOS), molecular electrostatic potential (MEP) of the two structures were investigated by theoretical calculations. Molecular properties such as Ionisation Potential (I), Electron affinity (A), chemical hardness (η), electronic chemical potential (μ) and electrophilicity (ω) obtained and three-centered intramolecular hydrogen bonding were investigated by NBO analysis.

Keywords: oxalyl; DFT; DOS; Natural charge; NBO analysis

INTRODUCTION

Oxamide derivatives are used as a model to study bonds in biomolecules, particularly intermolecular and intramolecular hydrogen bonding [1]. The hydrogen bond is a weak chemical bond between an electronegative atom, such as fluorine, oxygen or nitrogen and a hydrogen atom bound to another electronegative atom. Hydrogen bonds are responsible of water and many biological molecules [2-4]. These hydrogen-bond attractions can occur between molecules (intermolecular) or

within different parts of a single molecule (intramolecular) [5]. A three-center intramolecular hydrogen bonding interaction can be seen in all oxamides. Three-center intramolecular hydrogen bonding is bifurcated hydrogen bonding. There are two types of bifurcated hydrogen bonding in biological systems, organic compounds, that can be as intermolecular, intramolecular or both. One is three centered hydrogen bond where a electronegative atom participate as

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acceptor group and two hydrogen atoms as donor in two different hydrogen bonds, and the other kind is where two same electronegative atoms participate as acceptor groups and a hydrogen as acceptor atom [6].

In recent years, computational chemistry has become an important tool for chemists and a well-accepted partner for experimental chemistry [7-10]. Density functional theory (DFT) method has become a major tool in the methodological arsenal of computational organic chemists [11]. Isabel Rozas and et al. investigated bifurcated or three-centered hydrogen bonds (HB) using DFT (B3LYP/6-31G*) on different families of compounds such as monomers with intramolecular three-centered HB, dimers with a HB donor (HBD) and a molecule with two HB acceptor (HBA) groups, and trimers with one HBD and two HBAs [12]. A. Lakshmipriya et al. studied existence of three-centered C=O...H(N)...X-C hydrogen bond in diphenyloxamide derivatives involving halogens using NMR spectroscopy and quantum theoretical studies [13]. Martinez-Martinez reported synthesis of *N*-(2-benzoyl-phenyl) oxalyl derivatives [14]. Three crystal structures *N*-(2-benzoylphenyl) acetamide, *N*-(2-benzoylphenyl) oxalamate and *N1,N2*-bis(2-benzoylphenyl)oxalamide is reported by Carlos Z. Gomez-Castro et al [15]. They studied the formation of three-center hydrogen bonds in three oxalyl derivatives was by the X-ray diffraction analysis. In the present work, we investigate the energetic and structural properties of title two crystal structures (*N*-(2-benzoylphenyl) oxalamate and *N1,N2*-bis(2-benzoylphenyl)oxalamide) using DFT calculations. The optimized geometry, frontier molecular orbitals

(FMO), detail of quantum molecular descriptors, molecular electrostatic potential (MEP), chemical tensors, natural charge and three-center hydrogen bonds using NBO analysis were calculated.

COMPUTATIONAL METHODS

In this work, we have carried out quantum theoretical calculations for the compounds **I** and **II** using B3LYP/6-311+G* level (DFT) [16] by the Gaussian 03W program package [17] and calculate their properties. At first we have optimized structure using Gaussian 03W program (see Figure 1). We calculated NMR parameters such as chemical shift isotropic (CS^I) and chemical shift anisotropic (CS^A) for title structures using B3LYP/6-311+G* level [18,19]. The electronic properties such as E_{HOMO} , E_{LUMO} , HOMO-LUMO energy gap (ΔE), E_{HOMO-1} , E_{LUMO+1} , natural charges, molecular properties, dipole moment (μ_D) and point group were detected [20]. The optimized molecular structure, HOMO and LUMO surfaces were visualized using GaussView 03 program [21]. We also studied the thermodynamic parameters of molecules using the B3LYP/6-311+G* level, and obtained the energy (ΔE), enthalpies (ΔH), Gibbs free energy (ΔG), entropy (S) and constant volume molar heat capacity (C_v) of the structures [20,22]. The electronic structure of compounds **I** and **II** were studied by using Natural Bond Orbital (NBO) analysis at the same level in order to understand various second-order interactions between the filled orbitals of one subsystem and vacant orbitals of another subsystem, which is a measure of the inter-molecular delocalization or hyper conjugation [18]. We also is obtained the calculated natural charge (NBO) of three structures.

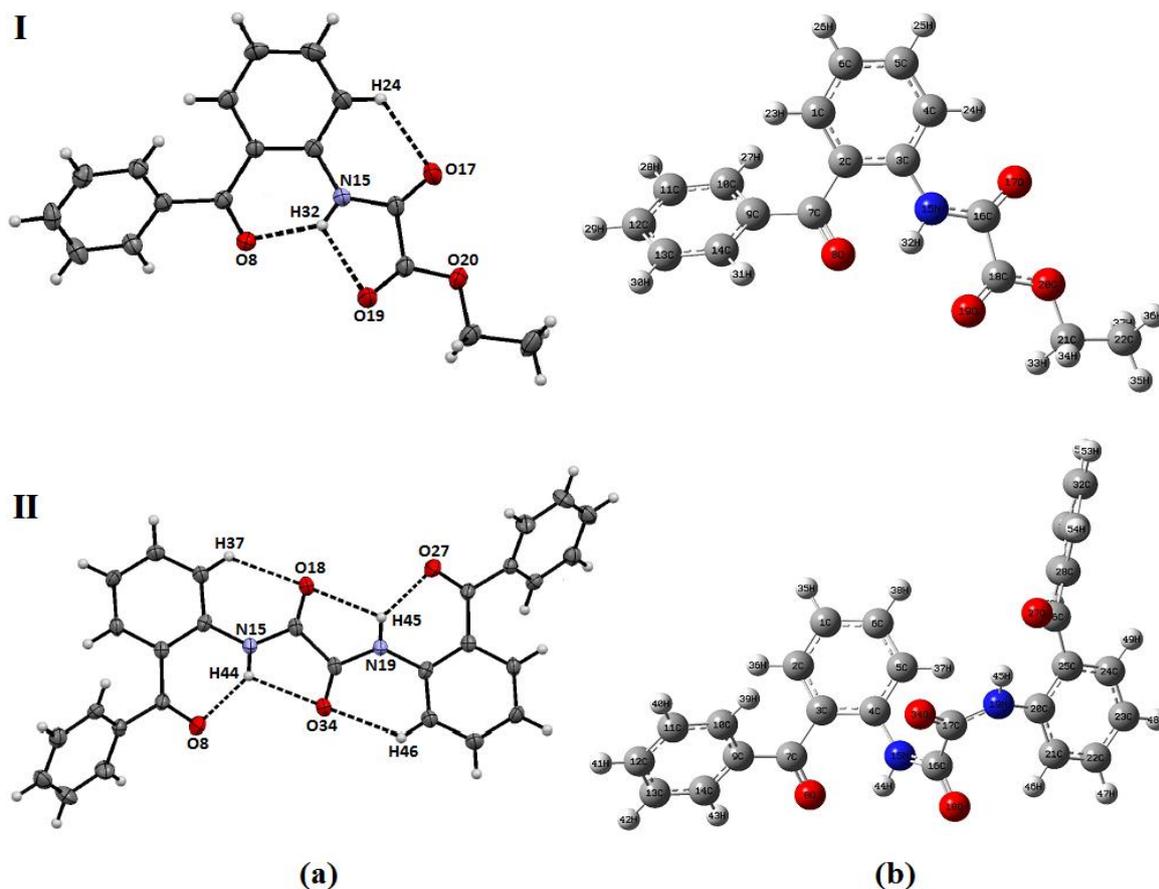


Fig. 1. (a) The Crystallographic numbering of the compounds **I** and **II**, (b) The theoretical geometric structure of the compounds **I** and **II** (optimized with B3LYP/6-311+G* level).

RESULTS AND DISCUSSION

Optimized geometry

The optimized structure of the molecules **I** and **II** has been calculated by DFT (B3LYP/6-311+G*) (see Figure 1) and the selected bond lengths and bond angles of the crystallographic structures¹⁵ and the theoretical parameters of listed in Table 1. As can be seen in Table 1, the calculated parameters show good approximation and can be used as a foundation to calculate the other parameters for the title compounds. We found that most of the calculated bond lengths are slightly longer than X-ray values that it is due to the fact that experimental result corresponds to interacting molecules in the crystal lattice, whereas computational method deals with

an isolated molecule in gaseous phase [23,24]. The average differences of the theoretical parameters from the experimental for bond lengths of compound **I** were found to be about 0.01Å (O₁₇-C₁₆), 0.001Å (O₈-C₇), 0.003Å (N₁₅-C₃), 0.02Å (N₁₅-C₁₆), 0.008Å (C₃-C₂), 0.006Å (C₂-C₇), 0.012Å (C₁₆-C₁₈), 0.004Å (C₇-C₉). According to Table 1, the bond length of N₁₅-C₃ in X-ray and optimized structure of compound **I** is 1.399Å and 1.402Å respectively, whereas experimental and theoretical value for the bond length of N₁₅-C₁₆ is 1.346Å and 1.366Å, respectively. It shown the bond length of N₁₅-C₁₆ is shorter than N₁₅-C₃ that it is due

to the fact that lone pair of N₁₅ conjugated with the C₁₆ (carbonyl group). Also according to Table 1, the average differences of the theoretical parameters from the experimental for bond lengths of compound **II** were found to be about 0.006Å (O₃₄-C₁₇), 0.004Å (O₈-C₇), 0.008Å (N₁₅-C₄), 0.018Å (N₁₅-C₁₆), 0.01Å (C₄-C₃), 0.012Å (C₃-C₇), 0.009Å (C₁₆-C₁₇), 0Å (C₇-C₉). As seen in Table 1, the bond length of N₁₅-C₄ in X-ray and optimized structure of compound **II** is 1.402Å and 1.410Å respectively, whereas experimental and theoretical value for the bond length of N₁₅-C₁₆ is 1.350Å and 1.368Å, respectively. It shown the bond length of N₁₅-C₁₆ is shorter than N₁₅-C₃ that it is due to the fact that lone pair of N₁₅ conjugated with the C₁₆ (carbonyl group).

Table 1. Selected bond lengths (Å) of the compounds **I** and **II** (atom labeling according to Fig. 1)

		Exp. ^a	Cal. ^b
I	O ₁₇ -C ₁₆	1.204(3)	1.214
	O ₈ -C ₇	1.227(2)	1.228
	N ₁₅ -C ₃	1.399(2)	1.402
	N ₁₅ -C ₁₆	1.346(2)	1.366
	C ₃ -C ₂	1.416(3)	1.425
	C ₂ -C ₇	1.486(2)	1.492
	C ₁₆ -C ₁₈	1.538(3)	1.550
	C ₇ -C ₉	1.496(2)	1.500
II	O ₃₄ -C ₁₇	1.211(4)	1.217
	O ₈ -C ₇	1.223(5)	1.227
	N ₁₅ -C ₄	1.402(4)	1.410
	N ₁₅ -C ₁₆	1.350(4)	1.368
	C ₄ -C ₃	1.407(4)	1.417
	C ₃ -C ₇	1.483(5)	1.495
	C ₁₆ -C ₁₇	1.548(5)	1.539
	C ₇ -C ₉	1.495(5)	1.495

^a Taken from Ref. [15].

^b Calculated using DFT method (B3LYP/6-311+G*)

In addition, the hydrogen bonds length values of experimental [15] and theoretical

compounds **I** and **II** summarized in Table 3. X-ray diffraction analysis of compound reveals that the structure is stabilized by intramolecular hydrogen bonding. According to experimental results is obtained by Carlos Z. Gómez-Castro, it revealed compound **I** has three intramolecular hydrogen bonding (see Figure 1) [15]. By knowing the bond length, the strength of the hydrogen bond can be determined as very strong (below 2.5Å), strong (2.5-2.7Å), normal (2.7-2.9Å) and weak (above 2.9Å). The first intramolecular hydrogen bonding of compound **I** [N₁₅-H₃₂...O₁₉], the experimental and theoretical values of bond length H₃₂...O₁₉ are 2.25Å and 2.23Å respectively, that suggesting the existence of very strong intramolecular hydrogen bond. In second intramolecular hydrogen bonding of compound **I** [N₁₅-H₃₂...O₈], the experimental bond length H₃₂...O₈ is 1.97Å and calculated value is 1.90Å. This suggesting the intramolecular hydrogen bond N₁₅-H₃₂...O₈ is very strong. In intramolecular three-centered hydrogen bond of O₁₉...H₃₂...O₈, the O₁₉...H₃₂ is weaker rather than H₂₅...O₈. The experimental and theoretical values of bond H₂₄...O₁₇ [C₄-H₂₄...O₁₇] is good evident for existence third intramolecular hydrogen bonding in structure **I**. According to Figure 1, there are two intramolecular three-centered hydrogen bonds [O₈...H₄₄...O₃₄ and O₁₈...H₄₅...O₂₇] in the theoretical geometric structure of **II**. The experimental and theoretical values for bond length of H₄₄...O₃₄ are 2.23Å and 3.84Å, respectively. As shown, the theoretical bond length of H₄₄...O₃₄ has which suggesting the existence of intramolecular hydrogen bond. The difference of the theoretical value from the experimental for intramolecular hydrogen bond length of H₄₄...O₃₄ [N₁₅-H₄₄...O₃₄] in compound **II** was found to be about 1.61Å. While the experimental and calculated

Table 2. Hydrogen-Bond Geometry (Å) (Exp.^a and Cal.^b) of compound **I** and **II**

	D-H...A	D-H (Å)		H...A(Å)		D...A(Å)	
		Exp.	Cal.	Exp.	Cal.	Exp.	Cal.
II	N15-H32...O19	0.86	1.02	2.25	2.23	2.666(2)	2.702
	N15-H32...O8	0.86	1.02	1.97	1.90	2.662(2)	2.703
	C4-H24...O17	0.93	1.08	2.29	2.18	2.908(3)	2.889
III	N15-H44...O34	0.86	1.02	2.23	3.84	2.665(4)	3.37
	N15-H44...O8	0.86	1.02	1.98	2.01	2.673(4)	2.742

a Taken from Ref. [15].

b Calculated using DFT method (B3LYP/6-311+G*)

values of intramolecular hydrogen bond length H₂₅...O₈ [N₁₅-H₄₄...O₈] are 1.98Å and 2.01Å respectively, that the difference of the theoretical value from the experimental is very low (about 0.03Å) and suggesting the intramolecular hydrogen bond N₁₅-H₄₄...O₈ is very strong.

Atomic charge and NMR parameters

We calculated the charge distributions for equilibrium geometry of molecules **I** and **II** by NBO method (natural charge) [25,26] using B3LYP/6-311+G* level. (Atoms labeling is according to Figure 1). The total charge of the investigated molecules is equal to zero. According to Table 3, the calculated results reveal the natural charges for H₂₄, H₃₂, H₃₃ and H₃₄ atoms in structure **I** are positive value (0.249e, 0.454e, 0.186e and 0.187e, respectively). Therefore the highest positive charge is observed for H₃₂ atom due to participate in forming three-centered intramolecular hydrogen bonding (O₁₉...H₃₂...O₈). Also H₂₄ atom participates in intramolecular hydrogen bonding with O₁₇ [C₄-H₂₄...O₁₇]. Therefore the charge value of H₂₄ atom is the most positive rather than H₃₃ and H₃₄ atoms. The highest values of negative charge is observed for N₁₅ atom (-0.607e). Also O₈, O₁₇, O₁₉ and O₂₀ atoms have high

negative charge (-0.580e, -0.577e, -0.588e and -0.524e, respectively). The C₁₈ atom has the most positive charge (0.734) that is due to link to electronegative O₁₉ and O₂₀ atoms. From calculated natural charge (NBO) is obtained for structure **II**, we found the highest values of negative charges are observed for N₁₅ and N₁₉ atoms, -0.617e and 0.622e, respectively. Also O₈, O₁₈, O₂₇ and O₃₄ atoms in structure **II** have high negative charge (-0.580e, -0.593e, -0.580e and -0.574e, respectively). The calculated natural charges for H₄₄ and H₄₅ atoms in structure **II** are high positive values (0.437e and 0.438e, respectively) that due to participate in forming three-centered intramolecular hydrogen bonding such as O₈...H₄₄...O₃₄ and O₁₈...H₄₅...O₂₇.

The NMR parameters such as chemical shift isotropic (CS^I) and chemical shift anisotropic (CS^A) for the molecules **I** and **II** are summarized in Table 3. In structure **I**, the CS^I values for H₂₄, H₃₂, H₃₃ and H₃₄ atoms is 23.031, 20.416, 28.102 and 28.072 ppm, respectively. As seen, H₃₂ atom has the lowest CS^I value (20.416 ppm) and highest CS^A value (10.774 ppm), therefore H₃₂ atom is the deshielder than other hydrogen atoms that it is as a result of forming three-centered intramolecular hydrogen bond [O₁₉...H₃₂...O₈]. Also

according to Table 1, in structure **II**, the CS^I values for H₃₇, H₄₄, H₄₅ and H₄₆ atoms is 25.354, 22.659, 22.298 and 23.620 ppm, respectively. As seen, H₄₄ and H₄₅ atoms have the lowest CS^I value (22.659 and 22.298 ppm, respectively) and highest CS^A value (13.276 and 11.868 ppm, respectively), therefore H₄₄ and H₄₅ atoms are the deshielder than other H₃₇ and H₄₆ atoms that it is as a result of forming three-

centered intramolecular hydrogen bond [O₈...H₄₄...O₃₄ and O₁₈...H₄₅...O₂₇].

Electronic properties

Quantum chemical methods are important to obtain information about molecular structure and electrochemical behavior. The Frontier Molecular Orbitals (FMO) analysis calculated for compounds using B3LYP/6-311+G* level [26]. The results

Table 3. The Natural Charge (NBO charges, e) and NMR parameters (ppm) such as chemical shift isotropic (CS^I) and chemical shift anisotropic (CS^A) for compounds **I** and **II** using B3LYP/6-311+G*level

	Natural Charge	CS^I (ppm)	CS^A (ppm)
<u>Compound I</u>			
C ₂	-0.169	54.297	185.975
C ₃	0.204	34.439	155.239
O ₈	-0.580	-276.578	921.097
N ₁₅	-0.607	110.860	152.232
C ₁₆	0.591	24.480	78.626
O ₁₇	-0.577	-93.434	669.744
C ₁₈	0.734	16.450	75.482
O ₁₉	-0.588	-72.104	586.068
O ₂₀	-0.524	106.128	145.793
H ₂₄	0.249	23.031	10.072
H ₃₂	0.454	20.416	10.774
H ₃₃	0.186	28.102	5.122
H ₃₄	0.187	28.072	5.220
<u>Compound II</u>			
C ₄	0.224	36.200	154.519
C ₇	0.555	-21.591	156.889
O ₈	-0.580	-279.263	925.461
N ₁₅	-0.617	106.531	111.484
C ₁₆	0.618	12.503	109.486
C ₁₇	0.614	13.730	101.805
O ₁₈	-0.593	-114.191	622.729
N ₁₉	-0.622	105.804	122.701
O ₂₇	-0.580	-277.384	930.478
O ₃₄	-0.574	-113.389	599.195
H ₃₇	0.212	25.354	5.377
H ₄₄	0.437	22.659	13.276
H ₄₅	0.438	22.298	11.868
H ₄₆	0.249	23.620	8.357

of FMO such as E_{HOMO} , E_{HOMO-1} , E_{LUMO} , E_{LUMO+1} and HOMO-LUMO energy gap (Eg) of molecules **I** and **II** are summarized in Table 7. The values of energy of the lowest unoccupied molecular orbital (LUMO) and the highest occupied molecular orbital (HOMO) [27]. The HOMO can act as an electron donor and the LUMO can act as the electron acceptor. A higher E_{HOMO} for the molecule indicates a higher electron-donating ability to an appropriate acceptor molecule with a low-energy empty molecular orbital [28]. As seen in Figure 6(a) charge transfer is taking place within molecules **I** and **II**. The graphic pictures of HOMO and LUMO orbitals show HOMO orbital of structure **I** is localized mainly on one of the phenyl rings and amid functional group, while LUMO orbital is focused mainly on phenyl rings, amid functional group and carbonyl group. The HOMO→LUMO transition implies an electron density transfer from one phenyl ring to another phenyl ring. The HOMO orbital of structure **II** is localized mainly on the two middle rings and two amid functional groups, whereas LUMO orbital is focused mainly on the two outer phenyl rings and two carbonyl groups.

Also in this work, electronic structure of compounds **I** and **II** was studied using total densities of states (DOSs) [29,30]. DOS plot shows population analysis per orbital and demonstrates a simple view of the character of the molecular orbitals in a certain energy range [31]. According to Figure 6(b), DOS analysis indicates calculated energy gaps (Eg) for molecules **I** and **II**. A large energy gap implies high stability for the molecule. According to Table 1, HOMO–LUMO energy gap (Eg) value of structure **I** (4.24 eV) is higher than of structure **II** (4.20 eV). Therefore structure **I** is less reactive rather than structures **II**.

A detail of quantum molecular

descriptors of structures **I** and **II** are summarized in Table 7. The I is Ionization potential ($I = -E_{HOMO}$) and A is Ionization potential and Electron affinity ($A = -E_{LUMO}$) [26]. The Chemical hardness ($\eta = (I - A)/2$) is important property to measure the molecular stability and reactivity [32]. A hard molecule has a large energy gap (Eg) and a soft molecule has a small energy gap (Eg) [33]. The Chemical hardness (η) values of structures **I** and **II** are 2.12 and 2.1 eV respectively, therefore structure **I** is a hard molecule and less reactive with high energy gap (Eg = 4.24 eV) rather than structure **II** (Eg = 4.19 eV). The electronic chemical potential ($\mu = -(I + A)/2$) is a form of the potential energy [The absorbed or released energy during a chemical reaction or change during a phase transition] [34]. The μ value of structure **II** is the most negative value (-4.59 eV) rather than structure **I** (-4.52 eV). The electrophilicity parameter (ω) show the stabilization in energy when the system acquires an additional electronic charge from the environment. The electrophilicity index ($\omega = \mu^2/2\eta$) contains information about both electron transfer (chemical potential) and stability (hardness) and is a better descriptor of global chemical reactivity [35]. The higher the value of electrophilicity index displays the high capacity of the molecule to accept electrons. The electrophilicity index for structures **I** and **II** is 4.82 and 5.02 eV, respectively. The structure **II** has the highest electrophilicity index, therefore it has high capacity for acceptance electrons. Dipole moment (μ_D) is a good measure for the asymmetric nature of a structure [26]. The size of the dipole moment depends on the composition and dimensionality of the 3D structures. As shown in Table 7, the dipole moment of structures **I** and **II** is 2.541 and 7.069 Debye. Therefore structure **II** has the highest value of dipole moment (7.069 Debye) which refers high

asymmetry in the structure and irregularly arranged which gives rise to the increased

dipole moment.

Table 4. Molecular properties of compounds **I** and **II** calculated using DFT (B3LYP/6-311+G*)

	E_{HOMO}	E_{LUMO}	E_{HOMO-1}	E_{LUMO+1}	E_g	I	A	μ	η	ω	μ_D	Point Group
I	-6.64	-2.4	-7.15	-1.72	4.24	6.64	2.4	-4.52	2.12	4.82	2.541	C1
II	-6.69	-2.49	-6.79	-2.36	4.20	6.69	2.49	-4.59	2.1	5.02	7.069	C1

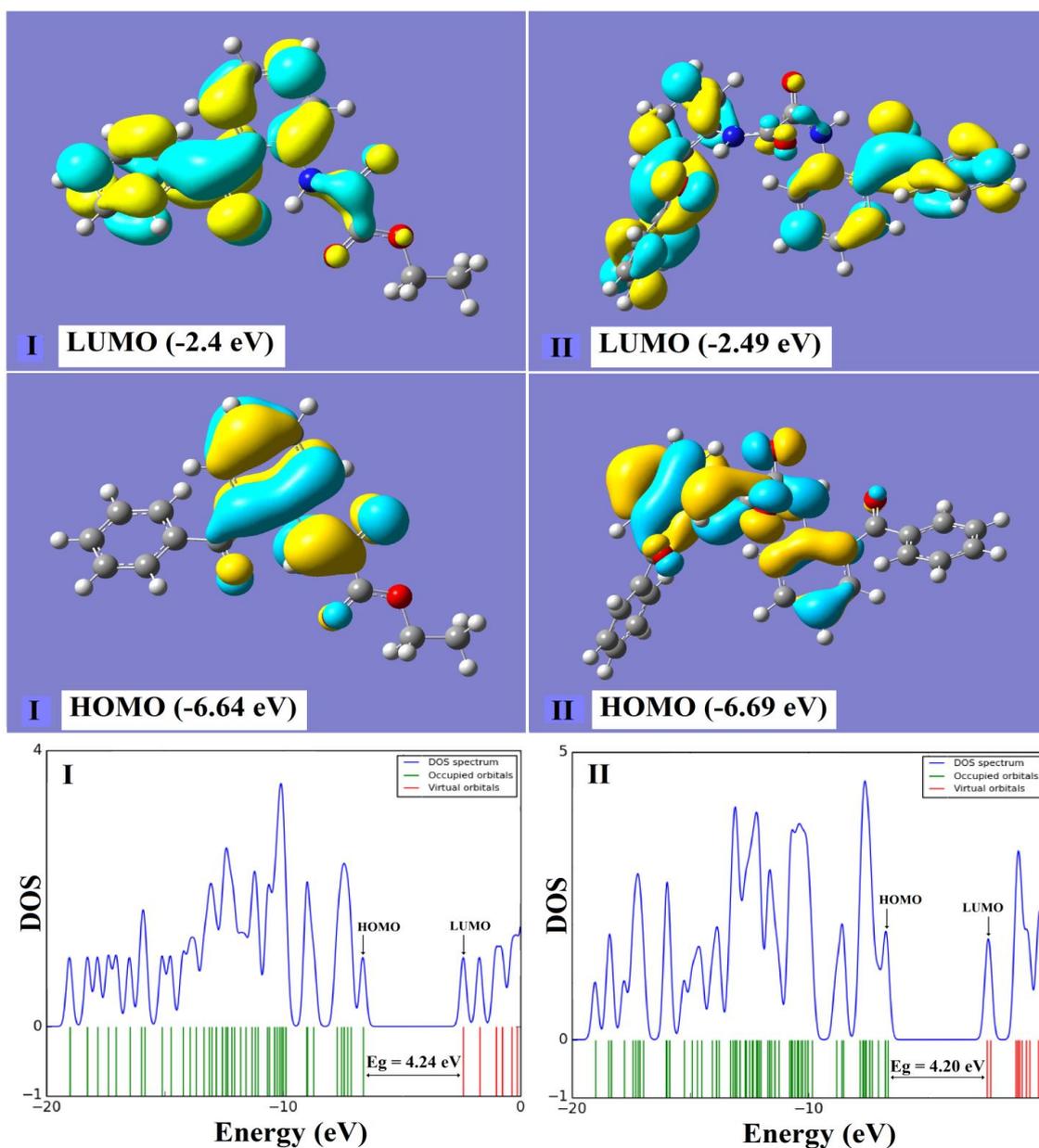


Fig. 2. Calculated Frontier molecular orbitals of structures **I** and **II** (ΔE : energy gap between LUMO and HOMO), (b): Calculated DOS plots of structures **I** and **II** (using B3LYP/6-311+G*).

Molecular electrostatic potential (MEP)

The molecular electrostatic potential (MEP) was checked out by theoretical calculations using B3LYP/6-311+G* level. Molecular electrostatic potential shows the electronic density and is useful in recognition sites for electrophilic attack and nucleophilic reactions as well as hydrogen bonding interactions [36,37]. The negative areas (red color) of MEP were related to electrophilic reactivity and the positive areas (blue color) ones to nucleophilic reactivity shown in Figure 7. Molecular electrostatic potential $V(r)$ [38] values are $-7.664e^{-2}$ for **I** and $-8.370e^{-2}$ for **II**. According to the MEP maps in Figure 7, negative region of compound **I** is mainly focused on O₈, O₁₇ and O₁₉ atoms with more color intensity (carbonyl groups). Therefore there are three positions on compound **I** for electrophilic attack. As shown in MEP map of the molecule **II**, the negative site is mainly focused on the O₁₈ and O₃₄ atoms (carbonyl groups). In structures **I** and **II**, hydrogen atoms of N-H groups are not suitable site for nucleophilic

activity (not blue color) that it is due to the fact that hydrogen atoms of N-H groups participate in the formation of intramolecular hydrogen bonding.

Thermodynamic Analysis

The relative energy (ΔE), standard enthalpies (ΔH), entropies (ΔS), Gibbs free energy (ΔG) and constant volume molar heat capacity (C_v) values of structures **I** and **II** were obtained by theoretical calculations using the B3LYP/6-311+G* level. Thermodynamic calculations indicate that the relative energies (ΔE), enthalpies (ΔH) and Gibbs free energy (ΔG) for compounds **I** and **II** are negative values while the calculated entropies (ΔS) are positive that indicate three molecules are stable in the gas phase (see Table 5). Also we found that the structure **II** has greater stability rather than structure **I** that due to existence six intramolecular hydrogen bondings in structure **II**, whereas structure **I** has three intramolecular hydrogen bonding.

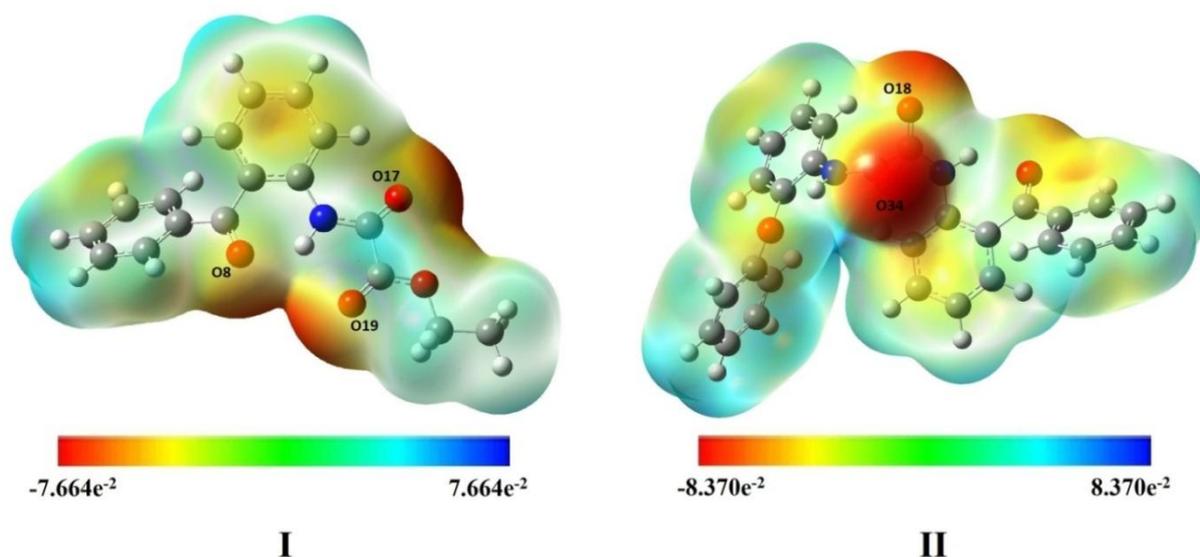


Fig. 3. Molecular electrostatic potential (MEP) maps of structures **I** and **II** calculated using B3LYP/6-311+G* level.

Table 5. Relative thermochemical parameters of structures **I** and **II** calculated using B3LYP/6-311+G* level

Compound	$\Delta E(\text{Kcal/mol})$	$\Delta G(\text{Kcal/mol})$	$\Delta H(\text{Kcal/mol})$	$\Delta S(\text{cal/molK})$	$C_v(\text{cal/molK})$
I	-635333.3424	-635377.7607	-635332.7500	150.967	73.249
II	-934592.8815	-934650.1737	-934592.2891	194.147	108.536

NBO analysis

Natural bond orbital (NBO) analysis is important method for studying intra- and inter-molecular bonding and interaction between bonds [39,40]. The results of NBO analysis such as the occupation numbers with their energies for the interacting NBOs and the polarization coefficient amounts of atoms for structures **I** and **II** are presented using B3LYP/6-311+G* level is summarized in Table 6. The size of polarization coefficients shows the importance of the two hybrids in the formation of the bond. According to Table 6, in structure **I**, the bonding orbital of the C₃-N₁₅ is $BD(1) = 0.6201sp^{2.67} + 0.7845sp^{1.75}$ and the N₁₅-C₁₆ is $BD(1) = 0.7915sp^{1.84} + 0.6112sp^2$. The polarization coefficients of two bonds C₃-N₁₅ and N₁₅-C₁₆ is shown importance of N₁₅ atom in forming these two bonds. Also the natural charge (NBO) of N₁₅ atom is more negative value (-0.607e) while C₃ and C₁₆ atoms are positive values (0.204e and 0.591e, respectively). Therefore more charge density resides on N₁₅ and is electron-rich. According to the calculated bonding orbitals for the C₇-O₈, C₁₆-O₁₇, C₁₈-O₁₉ and C₁₈-O₂₀, the polarization coefficients of oxygen atoms are greater than carbon atoms that it is shown importance of O₈, O₁₇, O₁₉ and O₂₀ in forming C₇-O₈, C₁₆-O₁₇, C₁₈-O₁₉ and C₁₈-O₂₀ bonds rather than C₇, C₁₆ and C₁₈ atoms. The calculated bonding orbital for the C₂-C₇ is $BD(1) = 0.7200sp^{2.24} + 0.6940sp^{1.83}$ with occupancy 1.97626a.u. and energy -0.67235a.u.. The polarization coefficient of C₂ (0.7200) is greater than C₇ (0.6940) that it shown

importance of C₂ atom in forming bond C₂-C₇ rather than C₇ atom. Also natural charge of C₂ atom is negative value (-0.169e) and C₇ atom positive value (0.548e). Therefore more charge density is focused on C₂ and is electron-rich. In structure **II**, the calculated bonding orbital for the C₇-O₈ bond is the $BD(1) = 0.5895sp^{2.35}d^{0.01} + 0.8078sp^{1.40}$ with high occupancy 1.99230a.u. and low energy -1.07618a.u.. The polarization coefficients of C₇= 0.5895 and O₈= 0.8078 are shown importance of O₈ atom in forming these bond and suggest that O₈ atom is more electron rich than the C₇ atom. The calculated natural charge (NBO) of O₈ atom is more negative (-0.580e) rather than C₇ atom (0.555e). Thus more the charge density resides on the O₈ atom. Also the polarization coefficients of other C-O bonds are shown importance of oxygen atom in forming these bonds. Also in the bonding orbital of the C₄-N₁₅ [$BD(1) = 0.6204sp^{2.80}d^{0.01} + 0.7843sp^{1.73}$] with high occupancy 1.98387a.u. and low energy -0.81031a.u., the polarization coefficient of C₄(0.6204) is greater than N₁₅(0.7843) that this suggest N₁₅ is more electron-rich (-0.617e) rather than C₄(0.224e). The bonding orbital of the C₁₆-C₁₇ is $BD(1) = 0.7071sp^{1.97} + 0.7072sp^{1.97}$. These polarization coefficients C₁₆(0.7071) and C₁₇(0.7072) shows importance both hybrids almost the same in the formation of the bond of C₁₆-C₁₇ bond. The calculated natural charges (NBO) of C₁₆ and C₁₇ atoms are positive values (0.618e and 0.614e, respectively).

Table 6. Calculated natural bond orbitals (NBO) and the polarization coefficient for each hybrid in selected bonds of compounds **I** and **II** using B3LYP/6-311+G* level

Energy (a.u.)	Bond (A-B) ^a	Occupancy (a.u.)	A	B
Compound I				
-0.70559	BD (1) C ₂ -C ₃	1.96909	0.7072 sp ^{1.95}	0.7070 sp ^{1.80}
-0.67235	BD (1) C ₂ -C ₇	1.97626	0.7200 sp ^{2.24}	0.6940 sp ^{1.83}
-0.65820	BD (1) C ₁₆ -C ₁₈	1.97172	0.7059 sp ^{2.11}	0.7083 sp ^{1.84}
-0.64558	BD (1) C ₂₁ -C ₂₂	1.99177	0.7132 sp ^{2.19}	0.7009 sp ^{2.45}
-0.81789	BD (1) C ₃ -N ₁₅	1.98629	0.6201 sp ^{2.67}	0.7845 sp ^{1.75}
-1.07311	BD (1) C ₇ -O ₈	1.99252	0.5898 sp ^{2.36} d ^{0.01}	0.8076 sp ^{1.41}
-1.08506	BD (1) C ₁₆ -O ₁₇	1.99399	0.5984 sp ^{1.89}	0.8012 sp ^{1.46}
-1.10569	BD (1) C ₁₈ -O ₁₉	1.99601	0.5929 sp ^{1.84}	0.8053 sp ^{1.48}
-0.95932	BD (1) C ₁₈ -O ₂₀	1.99225	0.5634 sp ^{2.36} d ^{0.01}	0.8262 sp ^{2.03}
-0.84621	BD (1) N ₁₅ -C ₁₆	1.98839	0.7915 sp ^{1.84}	0.6112 sp ²
Compound II				
-0.81031	BD (1) C ₄ -N ₁₅	1.98387	0.6204 sp ^{2.80} d ^{0.01}	0.7843 sp ^{1.73}
-1.07618	BD (1) C ₇ -O ₈	1.99230	0.5895 sp ^{2.35} d ^{0.01}	0.8078 sp ^{1.40}
-0.84725	BD (1) N ₁₅ -C ₁₆	1.98835	0.7907 sp ^{1.78}	0.6122 sp ^{2.04}
-0.66412	BD (1) C ₁₆ -C ₁₇	1.97490	0.7071 sp ^{1.97}	0.7072 sp ^{1.97}
-1.01239	BD (1) C ₁₆ -O ₁₈	1.99167	0.5943 sp ^{2.21} d ^{0.01}	0.8042 sp ^{1.76}
-1.04106	BD (1) C ₁₇ -O ₃₄	1.99094	0.5955 sp ^{2.14} d ^{0.01}	0.8033 sp ^{1.62}
-0.81447	BD (1) N ₁₉ -C ₂₀	1.98595	0.7839 sp ^{1.71}	0.6209 sp ^{2.70}
-1.08020	BD (1) C ₂₆ -O ₂₇	1.99233	0.5895 sp ^{2.36} d ^{0.01}	0.8077 sp ^{1.40}

^a A-B is the bond between atom A and atom B. (A: natural bond orbital and the polarization coefficient of atom; A-B: natural bond orbital and the polarization coefficient of atom B).

Electron donor orbital, acceptor orbital and the interacting stabilization energy resulting from the second-order micro disturbance theory [41] are reported in Table 7. The electron delocalization from filled NBOs (donors) to the empty NBOs (acceptors) describes a conjugative electron transfer process between them [42]. For each donor (*i*) and acceptor (*j*), the stabilization energy $E(2)$ associated with the delocalization $i \rightarrow j$ is estimated. The resonance energy ($E(2)$) detected the quantity of participation of electrons in the resonance between atoms.¹⁵ The results of the NBO analysis, such as resonance energy ($E(2)$), donor NBO (*i*) and acceptor NBO (*j*), for compound **I** and **II** using B3LYP/6-311+G* level are listed in Table 7. From results of the NBO analysis for compound **I**, the resonance energies ($E(2)$) of for LP(1)O₈→BD*(1)N₁₅-H₃₂ and LP(2)O₈→BD*(1)N₁₅-H₃₂ is 2.58 and 5.83 kcal/mol, respectively. These results

suggest existence a intramolecular hydrogen bond of O₈...H₃₂-N₁₅. The calculated natural charge of O₈ (-0.580e) and H₃₂ (0.454e) that are taking part in intramolecular charge transfer is indicated in the NBO analysis. Also LP(2)O₁₉ participates as donor and the anti-bonding BD*(1)N₁₅-H₃₂ orbital act as acceptor and their resonance energies ($E(2)$) is 1.41 kcal/mol that indicate charge transfer from the bonding orbital LP(2)O₁₉ to the anti-bonding orbital BD*(1)N₁₅-H₃₂ that is shown existence a intramolecular hydrogen bond of O₁₉...H₃₂-N₁₅. These results suggest forming three-centered intramolecular hydrogen bond O₈...H₃₂...O₁₉. In compound **I**, LP(1)N₁₅ orbital participates as donor and the anti-bonding BD*(2)C₂-C₃ and BD*(2)C₁₆-O₁₇ orbitals act as acceptor and their resonance energies ($E(2)$) is 37.94 and 62.57 kcal/mol respectively, that shown large charge transfer from the LP(1)N₁₅ to the anti-

bonding orbital of $BD^*(2)C_{16}-O_{17}$ [$LP(1)N_{15} \rightarrow BD^*(2)C_{16}-O_{17}$] rather than $BD^*(2)C_2-C_3$ orbital. As shown in Table 7, the resonance energies ($E(2)$) of $LP(1)O_{17} \rightarrow BD^*(1)C_4-H_{24}$ and $LP(2)O_{17} \rightarrow BD^*(1)C_4-H_{24}$ is 0.61 and 1.22 kcal/mol respectively, that shown existence interaction of $O_{17} \dots H_{24}-C_4$. The $LP(2)O_{20}$ orbital participates as donor and the anti-bonding $BD^*(2)C_{18}-O_{19}$, $BD^*(1)C_{21}-H_{33}$ and $BD^*(1)C_{21}-H_{34}$ orbitals act as acceptor and their resonance energies ($E(2)$) is 53.18, 4.31 and 4.25 kcal/mol, respectively. These values indicate large charge transfer from the $LP(2)O_{20}$ to anti-bonding orbital of $BD^*(2)C_{18}-O_{19}$ [$LP(1)N_8 \rightarrow BD^*(1)C_7-H_{25}$]. According to the results of the NBO analysis for compound **II**, the resonance energies ($E(2)$) for $LP(1)O_8 \rightarrow BD^*(1)N_{15}-H_{44}$ and $LP(2)O_8 \rightarrow BD^*(1)N_{15}-H_{44}$ is 1.45,

and 3.23 kcal/mol respectively, that suggest existence intramolecular hydrogen bond of $O_8 \dots H_{44}-N_{15}$. As shown in Table 7, the resonance energies ($E(2)$) of $LP(1)N_{19} \rightarrow BD^*(2)C_{17}-O_{34}$ and $LP(1)N_{19} \rightarrow BD^*(2)C_{20}-C_{21}$ is 50.11 and 25.63 kcal/mol, respectively. These values indicate large charge transfer from the $LP(1)N_{19}$ to anti-bonding orbital of $BD^*(2)C_{17}-O_{34}$ [$N_{19} \rightarrow C_{17}-O_{34}$]. Also the resonance energies ($E(2)$) of $LP(1)O_{27} \rightarrow BD^*(1)N_{19}-H_{45}$ and $LP(2)O_{27} \rightarrow BD^*(1)N_{19}-H_{45}$ is 1.78 and 4.19 kcal/mol respectively, that shown existence intramolecular hydrogen bond of $O_{27} \dots H_{45}-N_{19}$. The calculated natural charge of O_{27} ($-0.580e$) and H_{45} ($0.438e$) that are taking part in intramolecular charge transfer is indicated in the NBO analysis.

Table 7. Significant donor–acceptor interactions and second order perturbation energies of compounds **I** and **II** calculated using B3LYP/6-311+G* level

Donor NBO(i)	Acceptor NBO(j)	$E(2)^a$ (kcal/mol)	$E(j)-E(i)^b$ (a.u.)	$F(i, j)^c$ (a.u.)
Compound I				
$LP(1)O_8$	$BD^*(1)N_{15}-H_{32}$	2.58	1.11	0.048
$LP(2)O_8$	$BD^*(1)N_{15}-H_{32}$	5.83	0.69	0.058
$LP(1)N_{15}$	$BD^*(2)C_2-C_3$	37.94	0.28	0.093
	$BD^*(2)C_{16}-O_{17}$	62.57	0.27	0.119
$LP(1)O_{17}$	$BD^*(1)C_4-H_{24}$	0.61	1.15	0.024
$LP(2)O_{17}$	$BD^*(1)C_4-H_{24}$	1.22	0.72	0.027
$LP(2)O_{19}$	$BD^*(1)N_{15}-H_{32}$	1.41	0.69	0.029
$LP(2)O_{20}$	$BD^*(2)C_{18}-O_{19}$	53.18	0.33	0.118
	$BD^*(1)C_{21}-H_{33}$	4.31	0.71	0.052
	$BD^*(1)C_{21}-H_{34}$	4.25	0.71	0.052
Compound II				
$LP(1)O_8$	$BD^*(1)N_{15}-H_{44}$	1.45	1.10	0.036
$LP(2)O_8$	$BD^*(1)N_{15}-H_{44}$	3.23	0.68	0.043
$LP(1)N_{15}$	$BD^*(1)C_3-C_4$	2.62	0.77	0.044
	$BD^*(2)C_3-C_4$	25.64	0.28	0.77
	$BD^*(1)C_4-C_5$	2.10	0.81	0.040
	$BD^*(1)C_{16}-O_{18}$	1.93	0.82	0.39
	$BD^*(2)C_{16}-O_{18}$	43.32	0.33	0.109
$LP(1)O_{18}$	$BD^*(1)C_{21}-H_{46}$	0.80	1.15	0.036
$LP(2)O_{18}$	$BD^*(1)C_{21}-H_{46}$	0.73	0.71	0.021
$LP(1)N_{19}$	$BD^*(1)C_{17}-O_{34}$	0.71	0.85	0.024
	$BD^*(2)C_{17}-O_{34}$	50.11	0.30	0.113
	$BD^*(1)C_{20}-C_{21}$	1.83	0.82	0.038

Continued Table 7

	BD*(2) C ₂₀ -C ₂₁	25.63	0.28	0.076
	BD*(1) C ₂₀ -C ₂₅	2.55	0.79	0.044
LP (1) O ₂₇	BD*(1) N ₁₉ -H ₄₅	1.78	1.10	0.040
LP (2) O ₂₇	BD*(1) N ₁₉ -H ₄₅	4.19	0.68	0.049

^a E(2) means energy of hyperconjugative interactions.

^b Energy difference between donor and acceptor i and j NBO orbitals.

^c F(i, j) is the Fock matrix element between i and j NBO orbitals.

CONCLUSION

In the present study, the quantum theoretical calculations two crystal structures of *N*-(2-benzoyl-phenyl) oxalyl consists of three-centered intramolecular hydrogen bonding were performed using density functional theory method (DFT/B3LYP/6-311+G*). In structure **I**, the highest positive charge is observed for H₃₂ atom due to participate in forming three-centered intramolecular hydrogen bonding (O₁₉...H₃₂...O₈) and in structure **II**, the H₄₄ and H₄₅ atoms have high positive natural charges that due to participate in forming three-centered intramolecular hydrogen bondings such as O₈...H₄₄...O₃₄ and O₁₈...H₄₅...O₂₇. The CS^I value of the H₃₂ in structure **I** and H₄₄ and H₄₅ in structure **II** show these hydrogens are deshielder than other hydrogen atoms as a result of forming three-centered intramolecular hydrogen bond. Thermodynamic analysis indicates that structure **II** has greater stability rather than structure **I** that due to existence six intramolecular hydrogen bondings. According to the results of the NBO analysis for structure **I**, charge transfer LP(1)O₈→BD*(1)N₁₅-H₃₂ and LP(1)O₂₇→BD*(1)N₁₅-H₃₂ suggest forming three-centered intramolecular hydrogen bond O₈...H₃₂...O₁₉. FMO analysis suggests that charge transfer is taking place within the molecules **I** and **II**. The energy gap of structure **I** is higher than structure **II**, therefore structure **I** has the lowest reactivity.

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